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Uncertainty Modeling in Autonomous Vehicle Trajectory Prediction: A Comprehensive Survey

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Abstract

001 Agent Behavior prediction is a critical component in au-002 tonomous driving systems, requiring the modeling of inherent uncertainties in an agent's future motion. This 003 survey provides a comprehensive overview of uncer-004 tainty quantification approaches in agent behavior pre-005 006 diction, categorizing them into three main paradigms: probabilistic distribution-based models, generative mod-007 els, and heatmap-based representations. We analyze 008 how these paradigms address different aspects of uncer-009 010 tainty-including intent ambiguity, control variations, and inter-agent interactions—and evaluate their performance 011 across standard benchmarks. Our comparison reveals the 012 trade-offs between model expressiveness, computational ef-013 ficiency, and deployment practicality. We conclude by 014 identifying promising research directions that could ad-015 016 vance uncertainty-aware trajectory prediction, ultimately contributing to safer and more reliable autonomous driving 017 systems in complex real-world environments. 018

1. Introduction

020 Behavior prediction is a critical component to make self-021 driving cars work [26, 31]. In autonomous driving, behav-022 ior prediction forecasts the future trajectories and intentions of dynamic agents around the self-driving car. It is the pro-023 024 cess of forecasting how these dynamic agents, such as ve-025 hicles, pedestrians, or cyclists will move and interact based 026 on historical observations and contextual cues from the environment. It serves as a critical link between perception 027 (understanding the environment) and planning (determining 028 the next actions of the self-driving car). Accurate behav-029 ior prediction is fundamental to autonomous vehicle safety 030 and efficiency. Anticipating future agent actions allows self-031 032 driving cars to make proactive, risk-aware decisions, reducing accident likelihood and improving navigation in unpre-033 034 dictable urban environments

035 Future behavior prediction is inherently uncertain due to

the stochastic nature of real-world environments and human036decision-making. To illustrate this with an example, let us037consider the uncertainty in future behavior prediction from038the perspective of an agent navigating in the environment of039an autonomous vehicle.040

Intent Uncertainty This source of uncertainty comes 041 from the fundamental ambiguity in the agent's intent. [5, 042 30, 38] For instance, if an agent is waiting at an intersection 043 and originally planned to continue straight, they may sud-044 denly decide to make a right turn because their final desti-045 nation might change or because their intent changes. For 046 example, an agent intending to travel to a grocery store may 047 decide to make an additional stop at a gas station along the 048 route, potentially changing their trajectory mid-journey and 049 altering their final desired goal position. Modeling this un-050 certainty is inherently stochastic, meaning that even with 051 perfect models and unlimited data, we can never achieve 052 100% prediction accuracy due to the random nature of hu-053 man decision-making. 054

Control Uncertainty This source of uncertainty can arise even when the agent's intent is clear [5, 38]. Even if we are entirely certain that an agent is going to proceed straight, there remains growing uncertainty about its exact future pose. This uncertainty increases the further into the future we try to predict. Factors such as road conditions or subtle variations in pedal force applied by human drivers contribute to this growing pose uncertainty over time.

Interaction Uncertainty: This source of uncertainty arises from the complex interactions between multiple agents in a shared environment. For example, a vehicle that plans to accelerate may suddenly brake if another vehicle or pedestrian unexpectedly enters its path. Since agents operate within shared environments, their behaviors depend on responses from other agents, creating cascading uncertainties that make precise prediction of future behavior increasingly difficult as the number of interacting agents grows

From a machine-learning modeling perspective, these uncertainties can be categorized as *aleatoric* or *epistemic* [7, 10, 21, 22].

• Aleatoric uncertainty arises from the inherent stochas-

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ticity of the environment and represents randomness that 076 exists regardless of data quantity or model sophistication. 077 This type of uncertainty captures the unpredictable nature 078 of real-world systems where identical initial conditions 079 080 can lead to different outcomes. In autonomous driving, it manifests as the inherent unpredictability in human be-081 havior that cannot be eliminated even with perfect mod-082 eling. 083

084 • Epistemic uncertainty stems from the model's lack of knowledge and can be reduced through improved archi-085 086 tectures or increased data diversity. This uncertainty reflects limitations in model capacity or distributional shifts 087 between training and deployment environments. It be-088 comes particularly pronounced when encountering out-089 of-distribution samples, edge cases, or long-tail phenom-090 091 ena that were underrepresented in the training data.

Why is modeling uncertainty in behavior prediction crit-*ical for autonomous vehicle safety?* Modeling future agent
behaviors with uncertainty is a critical advancement in autonomous vehicle systems.

Earlier prediction systems produced only a single 'best' 096 trajectory, often resulting in unrealistic interpolations that 097 misled autonomous vehicle planners. For instance, when 098 an agent had multiple valid choices (e.g., going straight or 099 turning right), models sometimes generated an implausible 100 diagonal path [1, 3, 16, 23, 28, 32]. This could lead to 101 poor planning decisions, increasing the risk of unexpected 102 lane deviations and potential collisions. This could result 103 in a trajectory cutting across lanes or medians-one that 104 105 no reasonable driver would actually follow. This limitation indicates that earlier models lacked the fundamental 106 capability to represent behavioral uncertainty. The conse-107 quential impact emerged in how downstream systems in au-108 tonomous vehicles processed these predictions. When pre-109 sented with only a single trajectory devoid of uncertainty 110 111 information, the self-driving car could only perform binary collision detection against this "average" path. The au-112 113 tonomous vehicle would then use this limited binary collision assessment to attempt planning a collision-free path, 114 despite being based on potentially unrealistic agent predic-115 tions. This methodology introduces significant risk and rep-116 resents a rudimentary approach to collision assessment. To 117 compensate for these limitations, practical implementations 118 required numerous heuristics to enhance robustness and ac-119 120 curacy of collision detection algorithms. The introduction of uncertainty modeling eliminates the need for these 121 heuristic approaches. Probabilistic trajectory representa-122 tions allow systems to shift from binary collision detection 123 to a more informative 'probability of collision' assessment. 124 This probabilistic framework provides autonomous vehicles 125 with substantially improved capabilities for quantifying col-126 lision risks when interacting with multiple agents. 127

128 The growing importance of uncertainty-aware trajectory

prediction in autonomous driving has led to significant re-129 search advances in recent years. Various approaches have 130 emerged to address the fundamental challenge of represent-131 ing and quantifying uncertainty in agent behavior. To sys-132 tematically explore these developments, we present a com-133 prehensive analysis of uncertainty modeling techniques in 134 trajectory prediction. This work is structured around these 135 key components: 136

- Section 2 presents an overview of different paradigms for quantifying uncertainty in trajectory prediction, including probabilistic distributions, generative approaches, and heatmap-based representations.
- Section 3 delivers an in-depth survey of various models in recent literature categorized by these uncertainty quantification approaches, analyzing their theoretical foundations, implementation techniques, and how they address both aleatoric and epistemic uncertainty in autonomous driving contexts.
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- Sections 4 and 5 provide a quantitative comparison across benchmark datasets and outline promising future research directions, respectively.

Key Contributions:

- A structured taxonomy of uncertainty quantification paradigms for trajectory prediction.
- A comparative analysis of state-of-the-art models based on accuracy, uncertainty calibration, and deployment feasibility.
- Insights into open challenges and future research directions, focusing on hybrid modeling strategies and realworld integration.

2. Background on Uncertainty Quantification 159 Paradigms 160

This section provides an overview of the major paradigms161for quantifying uncertainty in behavior prediction.162

2.1. Probabilistic Distribution-Based Models

Probabilistic models for behavior prediction typically repre-
sent an agent's intent uncertainty by defining a fixed set of
possible futures the agent might choose. Each future corre-
sponds to a distinct high-level decision (e.g., going straight,
turning left), and a probability distribution is assigned over
these modes.164
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A common approach is to predefine a set of trajectory 170 anchors that serve as representative modes of future mo-171 tion. Figure 1 demonstrates an example of this from the 172 MultiPath [5] paper. Given an observed history, the model 173 predicts the probability of each anchor being chosen, along 174 with deviations from the anchor trajectory. This formu-175 lation provides a structured way to capture multi-modal 176 uncertainty while maintaining a compact representation. 177 [5, 29, 35]178



Figure 1. Probabilistic distribution-based models represent uncertainty through multiple trajectory anchors with associated probabilities. Left: Individual anchors with varying probability values (p). Right: Complete set of K = 16 anchors showing the multimodal distribution. Figure adapted from [5].

Beyond intent uncertainty, some probabilistic models
also explicitly model *control uncertainty*, which accounts
for variations in trajectory execution even when the intent is
fixed. This is typically modeled as a probability distribution
over trajectory refinements, allowing the model to express
deviations due to environmental factors, agent dynamics, or
perception noise. [5]

Most probabilistic models follow a marginal prediction 186 187 approach, where each agent's trajectory is predicted independently without explicitly modeling interactions. While 188 this simplifies computation and training, it does not inher-189 ently capture interaction uncertainty, where the future mo-190 tion of one agent is conditioned on that of others. Some 191 192 probabilistic models attempt to address this limitation by 193 incorporating interaction-aware mechanisms, but handling joint uncertainty remains an open challenge [27]. 194

195 2.2. Generative Models for Uncertainty Modeling

Generative models for behavior prediction produce a distri-196 bution over possible future trajectories of an agent through 197 sampling-based approaches. Typically, these models sam-198 ple multiple seeds from a normal distribution to generate 199 200 plausible futures that reflect both intent and control uncertainty. Since these models generate sample trajectories of 201 202 all agents in the environment at once from a given seed, they provide interaction-aware predictions. This contrasts 203 204 with most Probabilistic Distribution-Based Models, which generally only perform marginal trajectory prediction. Fig-205 ure 2 demonstrates an example of this approach from the 206 Trajectron++ [33] paper which models multi-agent interac-207 tions between pedestrians, showing how multiple possible 208 trajectories are predicted while accounting for inter-agent 209 210 influences. [4, 14, 15, 20, 33, 34, 36]



Figure 2. Generative models use structured representations to model interaction uncertainty, ensuring sampled trajectories remain consistent. Figure adapted from [33].

2.3. Heatmap-Based Representations

Heatmap-based models quantify uncertainty by predicting 212 spatial probability distributions over future agent positions 213 rather than discrete trajectory sets. Unlike probabilistic 214 models that define explicit probability distributions or gen-215 erative models that sample from a latent space, heatmap-216 based approaches produce a continuous probability field 217 over a spatial grid. Each pixel in the heatmap represents a 218 potential future position, with intensity values indicating the 219 likelihood of occupancy at that location. This formulation 220 naturally captures multi-modal uncertainty, as the spread of 221 high-probability regions corresponds to the range of pos-222 sible future motions. This is then followed by sampling 223 from the heatmap to generate trajectories. Figure 3 demon-224 strates an example of this approach from the HOME paper 225 which generates trajectory predictions by first creating spa-226 tial probability heatmaps and then sampling representative 227 paths with associated confidence scores while accounting 228 for interactions with other agents. [11–13, 19, 24] 229



Figure 3. HOME model visualization showing probability heatmaps, sampled trajectories with confidence scores, and interacting agents at an intersection. Figure adapted from [11].

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3. Taxonomy of Uncertainty QuantificationApproaches in Behavior Prediction

This section provides an in-depth survey of various models in recent literature categorized by their uncertainty quantification paradigms. The focus is on analyzing their theoretical foundations, implementation techniques, and how they address both aleatoric and epistemic uncertainty in autonomous driving contexts.

238 **3.1.** Probabilistic Distribution-Based Models

MultiPath [5] models uncertainty in behavior prediction by 239 representing future motion as a discrete distribution over 240 predefined anchor trajectories with Gaussian-distributed 241 offsets. It explicitly separates intent uncertainty from con-242 trol uncertainty. Intent uncertainty is modeled as a discrete 243 probability distribution over trajectory anchors. Control un-244 certainty is captured using normally distributed offsets at 245 each timestep, where the mean represents deviation from 246 the predefined anchor trajectory and the covariance repre-247 sents control uncertainty. 248

MultiPath++ [35] extends MultiPath by refining how 249 250 multimodal uncertainty is captured and aggregated. Instead 251 of relying on static trajectory anchors, it learns latent anchor embeddings, improving adaptability to diverse driving 252 contexts. Uncertainty is modeled using a Gaussian Mixture 253 Model (GMM), where multiple predicted trajectories are as-254 signed probabilities to represent stochastic human behavior. 255 256 To further enhance uncertainty modeling, MultiPath++ em-257 ploys an Expectation-Maximization (EM)-based clustering 258 algorithm, which aggregates multiple predictor outputs into a structured representation of future motion. This cluster-259 ing mechanism ensures that the final trajectory predictions 260 remain diverse while maintaining high-confidence probabil-261 ity estimates, leading to more calibrated and reliable multi-262 modal predictions compared to direct sampling-based ap-263 proaches. This approach reduces one of the critical prob-264 lems of intent mode collapse faced by MultiPath. 265

Target-driven trajectory prediction (TNT) [38] models 266 uncertainty by explicitly structuring trajectory generation 267 into two stages: target selection and motion estimation. 268 269 In the first stage, the model predicts a probability distri-270 bution over discrete target locations, capturing intent uncertainty by representing the likelihood of different high-271 level decisions. Given a selected target, the second stage 272 estimates continuous trajectories conditioned on that tar-273 get, assuming a unimodal distribution per target. This de-274 275 composition enables clear separation between uncertainty 276 in decision-making and uncertainty in execution, improving interpretability. The model further refines uncertainty 277 278 representation by applying a ranking mechanism and nonmaximum suppression-like filtering to eliminate redun-279 280 dant trajectory hypotheses while ensuring diverse, highlikelihood predictions.

Scene Transformer [27] explicitly models control uncer-282 tainty in multi-agent trajectory prediction by parameteriz-283 ing each predicted trajectory with a Laplace distribution, al-284 lowing it to capture variations in motion at each timestep. 285 Unlike models that predict independent agent trajectories, 286 Scene Transformer ensures joint consistency by applying 287 self-attention across agents and time steps, enabling more 288 structured uncertainty propagation. To improve efficiency, 289 it factorizes attention into temporal and agent-specific com-290 ponents, ensuring that uncertainty estimates remain coher-291 ent across interacting agents. 292

3.2. Generative Models

Social GAN [15] models uncertainty by generating multiple plausible future trajectories through adversarial learning. The generator produces trajectory samples, while the discriminator evaluates their realism based on social interactions. Social GAN uses a variety loss to encourage diverse predictions and prevent mode collapse. The diversity of sampled trajectories implicitly represents stochastic motion uncertainty, allowing the model to account for the variability in agent behavior while maintaining social compliance.

Trajectron++ [33] captures uncertainty using a Conditional Variational Autoencoder (CVAE), where a discrete latent variable encodes multiple plausible futures. By sampling from this latent distribution, the model captures both high-level intent uncertainty (decision-making variability) and low-level execution uncertainty (trajectory deviations). Instead of predicting deterministic future paths, Trajectron++ outputs a distribution over possible trajectories, where the spread of sampled trajectories reflects the model's confidence in its predictions. Additionally, uncertainty is propagated through probabilistic control distributions over acceleration and steering, ensuring dynamically feasible outputs.

FloMo (Flow-based Motion Prediction) [34] uses a nor-317 malizing flow-based approach to model uncertainty by 318 treating motion prediction as a density estimation problem, 319 learning a multimodal probability distribution over future 320 trajectories. Instead of generating discrete trajectory sets, 321 FloMo learns a direct transformation from a base noise dis-322 tribution to the trajectory space, ensuring both diverse and 323 probabilistically meaningful predictions. This approach en-324 ables efficient sampling of future trajectories while main-325 taining tractability in likelihood computation, making it par-326 ticularly effective for uncertainty-aware motion planning. 327 Additionally, FloMo introduces a likelihood-based training 328 method, addressing common issues such as mode collapse 329 in GANs and indirect uncertainty estimation in VAEs. To 330 ensure stability, FloMo incorporates a noise-injection tech-331 nique, which prevents likelihood spikes and enables robust 332

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333 generalization to real-world driving scenarios.

334 With the success of *Denoising Diffusion Probabilistic* 335 Models (DDPMs) [18] in various domains, this approach 336 has been extended into behavior prediction through Motion-Diffuser [20]. MotionDiffuser captures uncertainty through 337 a diffusion-based generative process, where noisy initial tra-338 jectory samples are iteratively refined into structured pre-339 dictions. Unlike GANs or VAEs, which generate trajecto-340 ries in a single step, MotionDiffuser starts from a Gaussian 341 noise distribution and progressively denoises it over mul-342 tiple iterations, ensuring controlled and diverse trajectory 343 generation. By conditioning this denoising process on past 344 motion and scene context, MotionDiffuser produces mul-345 timodal trajectory distributions that reflect inherent uncer-346 tainty while maintaining physical plausibility. This iterative 347 refinement enables fine-grained uncertainty representation. 348

349 3.3. Heatmap-Based Representations

Heatmap output for future motion estimation (HOME) [11] 350 351 represents uncertainty in trajectory forecasting using a 2D probability heatmap, where each pixel encodes the likeli-352 hood of an agent occupying that position in the future. Un-353 354 like methods constrained to predefined trajectory clusters, HOME captures the full distribution of possible outcomes, 355 356 supporting flexible multimodal predictions. To refine uncertainty representation, HOME integrates attention mecha-357 358 nisms that model inter-agent interactions, ensuring that pre-359 dicted probability distributions reflect realistic behavioral variations. Additionally, it introduces two sampling strate-360 gies for trajectory extraction: one that prioritizes coverage 361 362 to minimize the probability of missing the true future position and another that optimizes for final displacement accu-363 racy. This enables a trade-off between trajectory diversity 364 and precision without requiring retraining, making HOME 365 well-suited for adaptive motion forecasting in autonomous 366 driving applications. 367

368 Graph-oriented heatmap output for future motion esti-369 mation (GOHOME) [13] improves upon standard heatmapbased representations by incorporating lane connectivity in-370 formation, ensuring that trajectory predictions align with 371 real-world road constraints. Instead of computing a prob-372 373 ability distribution over a free-space grid, GOHOME gen-374 erates lane-level probability rasters and projects them onto a global heatmap, preserving road structure and traffic flow 375 376 patterns. By ranking the most probable lanelets and computing heatmaps only for those regions, GOHOME main-377 378 tains multimodal uncertainty representation while reducing 379 computational overhead. Additionally, the model employs 380 uncertainty-aware ensembling, combining multiple probability maps to enhance prediction accuracy while prevent-381 382 ing mode collapse, a common issue in trajectory-based forecasting. This structured approach allows GOHOME to cap-383 384 ture both aleatoric and epistemic uncertainty while maintaining computational efficiency, making it particularly effective for structured, long-horizon trajectory prediction.

Trajectory heatmap output with learned multi-agent 387 sampling (THOMAS) [12] refines heatmap-based uncer-388 tainty modeling by using a hierarchical decoding process 389 that iteratively refines predictions at multiple resolutions. 390 Instead of generating a single high-resolution probability 391 map, THOMAS begins with a coarse-grained heatmap to 392 approximate the overall uncertainty distribution and then 393 progressively refines it by focusing on high-probability 394 regions. This hierarchical strategy improves both com-395 putational efficiency and prediction accuracy, concentrat-396 ing resources where they are most needed. Additionally, 397 THOMAS employs a deterministic sampling mechanism to 398 extract diverse, multimodal trajectory endpoints from the 399 heatmap, ensuring that different future intentions and mo-400 tion variations are captured. To maintain scene consistency 401 across interacting agents, THOMAS introduces a modality 402 recombination module, which aligns agent trajectories to 403 prevent collisions and ensure that predictions remain jointly 404 coherent. This structured uncertainty modeling approach 405 makes THOMAS highly effective for multi-agent trajec-406 tory prediction, where maintaining scene-level consistency 407 is crucial for realistic and safe autonomous behavior. 408

4. Model Comparison and Analysis

This section presents a qualitative and quantitative comparison of uncertainty-aware trajectory prediction models410across standard benchmark datasets, evaluating their performance using standardized metrics that assess both accuracy412413414and uncertainty calibration.414

4.1. Qualitative Analysis

We propose a comprehensive framework for evaluating trajectory prediction paradigms across five critical dimensions that capture both the quality of uncertainty representation and practical system considerations:

- **Intent Uncertainty**: How well the approach captures the fundamental ambiguity in agent goals and intentions 421
- **Control Uncertainty**: The model's capacity to represent variability in trajectory execution given a fixed intent
- Interaction Uncertainty: How effectively the approach captures the interdependence between multiple agents' trajectories
- **Computational Efficiency**: The relative computational resources required for inference
- **Deployment Practicality**: Suitability for real-world implementation in autonomous systems

Table 1 presents our analysis of how the three major431paradigms—probabilistic models, generative approaches,432and heatmap-based methods—perform across these di-433mensions. Probabilistic models provide structured uncer-434

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435 tainty estimation but may struggle with modeling complex interactions. Generative approaches offer flexible and 436 437 interaction-aware predictions but suffer from stochasticity 438 and mode coverage issues, including intent mode collapse 439 (where the model fails to capture distinct, meaningful intent modes). Heatmap-based methods provide highly multi-440 modal spatial uncertainty representation but introduce com-441 putational complexity and require additional trajectory ex-442 443 traction steps. The choice of approach depends on system requirements, and future work may focus on hybrid strate-444 445 gies that combine the strengths of multiple paradigms.

446 4.2. Quantitative Analysis

The trajectory prediction field utilizes several benchmark 447 448 datasets for evaluation, with Argoverse [6] being one of the 449 most widely used due to its rich map data and diverse urban scenarios. Other notable datasets include Waymo Open Mo-450 tion Dataset [8], nuScenes [2], and INTERACTION [37], 451 each offering unique characteristics for specialized testing 452 scenarios. For our analysis, we focus on Argoverse, which 453 454 serves as a tracking benchmark with over 30K scenarios from Pittsburgh and Miami, sampled at 10 Hz, where each 455 sequence contains an agent whose future locations must be 456 predicted over a 3-second horizon. 457

To systematically evaluate model performance on this
benchmark, we consider both accuracy and uncertainty
quality metrics. Accuracy metrics measure how closely predicted trajectories align with actual movements:

- Minimum Final Displacement Error (minFDE) quantifies the final position error by selecting the closest prediction among multiple outputs.
- Minimum Average Displacement Error (minADE)
 computes the average deviation throughout the trajectory,
 capturing overall path alignment.
- 468 Miss Rate (MR) highlights critical prediction failures by
 469 counting instances where the predicted trajectory deviates
 470 beyond a predefined threshold, typically 2 meters for ve 471 hicles.

Uncertainty quality metrics assess how well models express confidence in their predictions:

- Brier-minFDE integrates accuracy and calibration, rewarding models whose confidence matches actual performance.
- 477 Diversity-Aware Coverage (DAC) evaluates how comprehensively predictions capture the range of plausible
 479 future motions, encouraging models to account for multiple possible outcomes rather than only the most probable
 481 one.

Table 2 presents the performance of various uncertaintyaware trajectory prediction models on the Argoverse Benchmark test dataset. HOME+GOHOME achieves the lowest miss rate (0.08), demonstrating superior performance in
capturing the most likely trajectories. MultiPath++ shows

the best overall accuracy with the lowest minFDE (1.21)and minADE (0.79), suggesting strong general prediction capability. Most models achieve near-perfect diversity coverage (DAC = 0.99) except for Social CVAE, which shows significantly worse performance across all metrics. This may indicate fundamental limitations in the pure CVAE approach when applied to complex driving scenarios. 487 490 490 491 492 493

It's worth noting that performance differences may also 494 relate to model complexity and computational resources, 495 not just algorithmic superiority. Models with larger param-496 eter counts or more sophisticated architectures may achieve 497 better results due to increased model capacity rather than 498 fundamental advancements in uncertainty modeling. Our 499 analysis focuses primarily on the uncertainty representation 500 capabilities rather than architectural details. 501

5. Conclusion and Future Directions

This survey has provided a comprehensive overview of un-503 certainty modeling approaches in trajectory prediction for 504 autonomous driving. We have categorized these approaches 505 into three main paradigms-probabilistic distribution-based 506 models, generative models, and heatmap-based representa-507 tions-and analyzed their theoretical foundations and im-508 plementation techniques. Each paradigm has strengths, but 509 deployment challenges persist, particularly in ensuring real-510 time inference under hardware constraints, handling edge 511 cases, and maintaining robustness in dynamic traffic envi-512 ronments. Addressing these issues is crucial for translat-513 ing uncertainty-aware trajectory prediction from research to 514 production-level autonomous systems. Probabilistic models 515 provide structured representations but often struggle with 516 complex interactions; generative approaches excel at cap-517 turing rich interaction dynamics but face deployment chal-518 lenges; and heatmap-based methods offer intuitive spatial 519 uncertainty representations but require additional process-520 ing steps. [9, 17, 25] 521

Future research should develop hybrid approaches that 522 integrate the interpretability of probabilistic models, the 523 flexibility of generative methods, and the multimodal rich-524 ness of heatmap-based approaches. Additionally, new 525 benchmarks should evaluate models not only on accuracy 526 and uncertainty calibration but also on real-time efficiency 527 and adaptability to domain shifts. Addressing these aspects 528 is essential for translating uncertainty-aware trajectory pre-529 diction into real-world autonomous systems. Additionally, 530 the field would benefit from standardized evaluation proto-531 cols specifically designed to assess uncertainty quality be-532 yond traditional accuracy metrics. Addressing these chal-533 lenges will require interdisciplinary efforts spanning ma-534 chine learning, robotics, and human behavior modeling, 535 ultimately enabling autonomous vehicles to safely navi-536 gate the complexity and unpredictability of real-world en-537 vironments. As uncertainty modeling techniques continue 538 to evolve, their integration into end-to-end autonomous 539

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Paradigm	Intent Uncertainty	Control Uncertainty	Interaction Uncertainty	Computational Effi- ciency	Deployment Practi- cality
Probabilistic Models	High Explicitly modeled using discrete trajectory modes	Moderate Gaussian offsets cap- ture variability, lacks fine-grained execution modeling	Low Typically models agents in- dependently, leading to in- teraction inconsistency	High Efficient due to dis- crete mode selection, low inference cost	High Widely used in real- world AV systems
Generative Mod- els	Moderate Latent variables encode di- verse intents, mode cover- age can be inconsistent	High Well-suited for stochastic motion modeling	High Jointly models agent inter- actions, producing socially consistent trajectories	Low Computationally expensive due to iterative sampling	Low Challenges for real- time deployment due to latency
Heatmap-Based Models	High Predicts spatial probability distributions, naturally cap- tures intent uncertainty	Moderate Some methods refine un- certainty via probability smoothing	High Well-suited for multi-agent interactions through shared spatial grids	Moderate Memory-intensive, re- quires trajectory post- processing	Moderate Used in research, but deployment remains challenging

Table 1. Comparison of uncertainty quantification paradigms in behavior prediction.

Model	minFDE	minADE	MR	Brier-minFDE	DAC
MultiPath++	1.21	0.79	0.13	1.79	0.99
TNT	1.45	0.91	0.17	2.14	0.99
Scene Transformer	1.23	0.80	0.13	1.89	0.99
HOME + GOHOME	1.29	0.89	0.08	1.86	0.98
THOMAS	1.44	0.94	0.10	1.97	0.98
Social CVAE	3.23	2.49	0.39	4.27	0.67

Table 2. Performance comparison of uncertainty-aware trajectory prediction models on Argoverse [6].

driving systems will play a crucial role in advancing the
safety, reliability, and performance of self-driving technologies.

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